Valence of Irreducible Polynomials over Rationals and over Finite Fields

Isaac Agyei

Ohio University, Athens, Ohio, United States

a joint work with

Sergio López-Permouth 1¹, Azam Mozaffarikhah 2², & Akuye-Shika Odametey 3.³

¹ Ohiol University, Athens, Ohio, United States

 2 Virginia University, Virginia, United States

³ Ohio University, Athens, Ohio, United States

Abstract

Abstract

We explore an extension of the algebra of polynomials on a single variable recently introduced in [1] by López-Permouth and Pallone, called algebras of m-nomials and entangled polynomials. We are motivated by the fact that there may exist non-trivial factorizations of irreducible polynomials within the context of entangled polynomials. We are interested in the notion of a positive integer $n \ (n \in \mathbb{Z}^+)$ such that f(x) *n*-nomial is reducible. The valence is the smallest $n \times n$ matrix such that it is possible to write the f(x) n-nomial as the product of two nonunits in $K^n[x]$. The valence can also be infinity if no such n exists. It was shown in [1] that linear polynomials have infinite valence. We explore possible ways in which the degree of a polynomial can influence its valence. We present, as a key element, how the determinant of a polynomial, when viewed as an nnomial via a finitistic representation also introduced in [1] helps determine the moment when irreducibility is lost. For this study, we focus on the cases when the underlying fields are rational or finite.

Keywords

Valence, Entangled Polynomial, *m*-nomial.

References

 López-Permouth, S. R., & Pallone, A. H. (2023). Rings of entangled polynomials. Rendiconti del Circolo Matematico di Palermo Series 2, 72(3), 1823-1843.

2