

ON HOLLOW-LIFTING SEMIMODULES

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a joint work with

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Abstract

The notions of lifting and hollow lifting modules are well studied in ring and module theory. Recently, many concepts in this theory were generalized in semiring and semimodule.

In this way, a left R -semimodule M is called hollow if for all proper subsemimodule of M is small in M and it is called lifting if for all subsemimodule N of M , there exists a direct summand K of M such that $N/K \ll M/K$. If M is lifting and M/N is hollow for all $N \leq M$, then M is called hollow-lifting.

In this work we introduce the notion of hollow-lifting semimodule and theirs characterisations. In an other hand we show when the concepts of hollow, lifting and hollow-lifting semimodules are equivalent.

Keywords

Subtractive semimodule, Lifting semimodule, Hollow-lifting semimodule, Local direct summand.

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